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## In the name of God, the Compassionate, the Merciful

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## Simulation of Light-Nanowire Interaction in the TE Mode Using Surface Integral Equations

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ABSTRACT— In this paper, the scattering of a plane monochromatic electromagnetic wave from a nanowire with circular cross-section in the transverse electric (TE) mode is simulated using the well-known Stratton-Chu surface integral equations. For an ordinary dielectric nanowire the refraction phenomenon is nicely simulated. In the case of a plasmonic nanowire no sign of surface plasmon excitation and propagation is seen. Transition from electrostatic regime to the geometrical shadow through diffraction regime by decreasing the light wavelength is also observable.

**KEYWORDS:** Light-nanowire interaction, Plasmonic nanowire, Stratton-Chu integral, TE mode.

## **I.INTRODUCTION**

Interaction of light with nanostructures is of fundamental importance from both theoretical and experimental points of view [1] and [2]. Many new subfields of nanotechnology such nano-plasmonics, micro-resonators. as photonic molecules, meta-materials, quantum dots, nano-lasers and etc lie in the field of light-nano interaction. Employing the quantum physics and related topics is inevitable to understand the exact mechanism of such interactions and to predict the results or justify the observations. However, in many cases, simple classical models are powerful enough and sufficient to study the interaction. In such cases, the nanostructure is modeled as a dielectric so that its interaction with light can classical easily be formulated using electrodynamics.

Depending on the dielectric function and the geometrical shape of the nanostructure and also the properties of its surrounding medium, the interaction problem can be solved analytically or numerically. Unfortunately, except for few simple configurations, there are no analytical solutions and therefore one should resort to numerical approaches. There are various and robust numerical methods concerning the light scattering from nanostructures. FDTD (Finite Difference Time Dipole DDA (Discrete Domain), Approximation) and SI (Surface Integral) algorithms are among the most famous methods each with its own advantages and drawbacks [3]-[5]. One of the advantages of SI methods is that they deal with lower spatial dimensions than the other volume approaches. Recently, SI methods, especially those based on Stratton-Chu surface integrals, have increasingly been employed to study lightnano interaction. They are really successful in simulating the fine details of the interaction. Using such methods, Rockstuhl et al. simulated the scattering of light from a plasmonic nanowire with elliptical crosssection and observed the excitation of localized surface plasmons [6]. Liaw et al. also simulated light scattering from various plasmonic nanowire configurations in transverse magnetic (TM) mode by a Startton-Chu based SI method with Boundary Element Method (BEM) [7] and [8]. They could illustrate excitation correctly the of propagating surface plasmons. However, they did not consider the interaction under TE

mode excitation. Other kinds of integral methods based on the *Green's* function have also been used by other researchers to simulate light-nano interaction [9] and [10].

In the present paper, following the method proposed in Liaw works, light scattering from a nanowire in TE mode is formulated and numerically solved for different nanowires. The paper is organized as follows: In the second section, coupled surface integral equations for TE mode are derived. The third section is devoted to the scattering from a simple and a plasmonic nanowire. Discussions and conclusions are presented in the two last sections.

## **II.** COUPLED SURFACE INTEGRAL EQUATIONS FOR TE MODE

A nanowire with arbitrary cross-section and with homogeneous and isotropic electric permittivity  $\varepsilon_2$  and magnetic permeability  $\mu_2$  is considered. It is placed in an infinite medium with homogeneous and isotropic electromagnetic constants  $\varepsilon_1$  and  $\mu_1$ . A plane monochromatic electromagnetic wave with frequency  $\omega$  is incident on the nanowire whose propagation direction is perpendicular to the wire axis. This is in fact a two-dimensional scattering problem. A cross-sectional cut of the configuration is shown in Fig. 1.



Fig. 1: Cross section of a nanowire (region  $\Omega_2$ ) with  $\varepsilon_2$  and  $\mu_2$  within an infinite medium (region  $\Omega_1$ ) with  $\varepsilon_1$  and  $\mu_1$ , irradiated with a electromagnetic plane wave.

The incident light can have any polarization, but, for two special cases the formulation will be simpler: 1) the transverse magnetic field (TM) mode in which the magnetic field of incident light is parallel to nanowire axis (here the 'z' axis), and, 2) the transverse electric field (TE) mode that its electric field is set along the nanowire. As mentioned before, the TM case was completely studied in [7] and [8] based on Stratton-Chu surface integral equations. Here, the TE mode with electric filed  $\mathbf{E}^{i}(\mathbf{r}) = \hat{\mathbf{e}}_{z} E_{z}^{i} e^{i\mathbf{k}\cdot\mathbf{r}}$  and magnetic induction  $\mathbf{B}^{i}(\mathbf{r}) = \left(\hat{\mathbf{e}}_{x}B_{x}^{i} + \hat{\mathbf{e}}_{y}B_{y}^{i}\right)e^{i\mathbf{k}\cdot\mathbf{r}}$  is considered. The superscript 'i' denotes the incident light,  $\hat{\mathbf{e}}_{x}$ ,  $\hat{e}_{v}$  and  $\hat{e}_{z}$  are Cartesian unit vectors and  $\mathbf{k} = \hat{\mathbf{e}}_{\mathbf{x}}k_{x} + \hat{\mathbf{e}}_{\mathbf{y}}k_{y}$  is the incident wave vector. In the SI methods, the unknown field values at any point of the space can be calculated from the known values of fields at boundary surfaces present in the problem. For TE mode there are three field unknowns in the space. They are  $E_z$ ,  $B_x$ , and  $B_y$  which denote electric field in 'z' direction and magnetic induction in 'x' and 'y' directions, respectively. Based on the Stratton-Chu surface integrals, the fields within the nanowire can be calculated from:

$$E_{z}(\mathbf{r}) = \int_{S} E_{z}(\mathbf{r'}) \, \hat{\mathbf{n}}' \cdot \nabla' G_{2}(\mathbf{r}, \mathbf{r'}) dr' - i\omega \int_{S} \mu_{2} H_{t}(\mathbf{r'}) G_{2}(\mathbf{r}, \mathbf{r'}) dr' + \mathbf{H}(\mathbf{r}) = -i\omega \int_{S} \varepsilon_{2} G_{2}(\mathbf{r}, \mathbf{r'}) E_{z}(\mathbf{r'}) d\mathbf{r'} + \frac{1}{\mu_{2}} \int_{S} B_{n}(\mathbf{r'}) \nabla' \mathbf{G}_{2}(\mathbf{r}, \mathbf{r'}) dr' - \int_{S} H_{t}(\mathbf{r'}) \, \hat{\mathbf{e}}_{z} \times \nabla' \mathbf{G}_{2}(\mathbf{r}, \mathbf{r'}) dr', \quad \mathbf{r} \in \Omega_{2}$$

$$(1)$$

and the fields out of it from:

$$E_{z}(\mathbf{r}) = E_{z}^{i}(\mathbf{r}) + \int_{S} E_{z}(\mathbf{r'}) \, \hat{\mathbf{n}}' \cdot \nabla' G_{1}(\mathbf{r}, \mathbf{r'}) \, dr' + i\omega \int_{S} \mu_{1} H_{t}(\mathbf{r'}) \, G_{1}(\mathbf{r}, \mathbf{r'}) \, dr'$$

$$\mathbf{H}(\mathbf{r}) = \mathbf{H}^{\mathbf{i}}(\mathbf{r}) + i\omega \int_{S} \varepsilon_{1} G_{1}(\mathbf{r}, \mathbf{r}') E_{z}(\mathbf{r}') \, \mathbf{d}\mathbf{r}' + \frac{1}{\mu_{1}} \int_{S} B_{n}(\mathbf{r}') \nabla' G_{1}(\mathbf{r}, \mathbf{r}') \, dr' - \int_{S} H_{t}(\mathbf{r}') \, \hat{\mathbf{e}}_{\mathbf{z}} \times \nabla' G_{1}(\mathbf{r}, \mathbf{r}') \, dr' \quad , \ \mathbf{r} \in \Omega_{1}$$

$$(2)$$

where  $\hat{\mathbf{n}}$ ,  $H_t$ , and  $B_n$  are normal unit vector, tangential component of magnetic field and normal component of magnetic induction at the nanowire surface *S*, respectively.  $G_1$  and  $G_2$  are Green's functions for the surrounding medium and the nanowire, respectively:

$$G_{j}(\mathbf{r},\mathbf{r}') = \frac{i}{4} H_{0}^{(1)}(k_{j} | \mathbf{r} - \mathbf{r}' |) , \quad j = 1, 2$$
 (3)

where  $H_0^{(1)}$  is the zero order Hankel's function of the first kind and  $k_j = \omega \sqrt{\varepsilon_j \mu_j}$  is the wave number. If the observation point approaches the boundary surface from both interior and exterior regions then Eqs. (1) and (2) yield:

$$\frac{1}{2}E_{z}(\mathbf{r}) = \int_{S} E_{z}(\mathbf{r}') \, \hat{\mathbf{n}}' \cdot \nabla' G_{2}(\mathbf{r}, \mathbf{r}') \, dr' - i\omega \int_{S} \mu_{2} H_{t}(\mathbf{r}') G_{2}(\mathbf{r}, \mathbf{r}') \, dr'$$

$$\frac{1}{2}\mathbf{H}(\mathbf{r}) = -i \, \omega \int_{S} \varepsilon_{2} \, \mathbf{G}_{2}(\mathbf{r}, \mathbf{r}') E_{z}(\mathbf{r}') \, \vec{dr}' + \frac{1}{\mu_{2}} \int_{S} B_{n}(\mathbf{r}') \, \nabla' G_{2}(\mathbf{r}, \mathbf{r}') \, dr' - \int_{S} H_{t}(\mathbf{r}') \, \hat{\mathbf{e}}_{z} \times \nabla' G_{2}(\mathbf{r}, \mathbf{r}') \, dr', \, \mathbf{r} \in S$$

and:

$$\frac{1}{2}E_{z}(\mathbf{r}) = E_{z}^{i}(\mathbf{r}) + \int_{S}E_{z}(\mathbf{r}')\,\hat{\mathbf{n}}'\,\cdot\,\nabla'G_{1}(\mathbf{r},\mathbf{r}')\,dr' + i\omega\int_{S}\mu_{1}\,H_{t}(\mathbf{r}')G_{1}(\mathbf{r},\mathbf{r}')\,dr'$$

$$\frac{1}{2}\mathbf{H}(\mathbf{r}) = \mathbf{H}^{\mathbf{i}}(\mathbf{r}) + i\omega \int_{S} \varepsilon_{1} G_{1}(\mathbf{r}, \mathbf{r}') E_{z}(\mathbf{r}') d\mathbf{r}' + \frac{1}{\mu_{1}} \int_{S} B_{n}(\mathbf{r}') \nabla' G_{1}(\mathbf{r}, \mathbf{r}') dr' - \int_{S} H_{t}(\mathbf{r}') \hat{\mathbf{e}}_{z} \times \nabla' G_{1}(\mathbf{r}, \mathbf{r}') dr', \ \mathbf{r} \in S$$
(5)

In Eqs. (4) and (5)  $\mathbf{r}$  and  $\mathbf{r'}$  are respectively the observation point and the integration variable both located at the nanowire surface. Equating tangential component of  $\mathbf{E}$ , tangential component of  $\mathbf{H}$  and normal component of  $\mathbf{B}$  from the interior and the exterior formulae at the surface, yields the following coupled surface integral equations:

$$E_{z}(\mathbf{r}) = E_{z}^{i}(\mathbf{r}) - \int_{S} E_{z}(\mathbf{r}')\hat{\mathbf{n}}' \cdot \nabla' [G_{1} - G_{2}] dr' + i\omega \int_{S} [\mu_{1}G_{1} - \mu_{2}G_{2}] H_{t}(\mathbf{r}') dr',$$

$$B_{n}(\mathbf{r}) = B_{n}^{i}(\mathbf{r}) + i\omega \int_{S} E_{z}(\mathbf{r}') [\mu_{1}\varepsilon_{1}G_{1} - \mu_{2}\varepsilon_{2}G_{2}]\hat{\mathbf{n}} \cdot d\mathbf{r}' - \int_{S} B_{n}(\mathbf{r}')\hat{\mathbf{n}} \cdot \nabla' [G_{1} - G_{2}] dr' + \int_{S} H_{t}(\mathbf{r}') \hat{\mathbf{n}} \cdot \hat{\mathbf{e}}_{z} \times \nabla' [\varepsilon_{1}G_{1} - \varepsilon_{2}G_{2}] dr',$$

$$H_{t}(\mathbf{r}) = H_{t}^{i}(\mathbf{r}) + i\omega \int_{S} E_{z}(\mathbf{r}') [\varepsilon_{1}G_{1} - \varepsilon_{2}G_{2}] \hat{\mathbf{t}} \cdot d\mathbf{r}' - \int_{S} B_{n}(\mathbf{r}') \hat{\mathbf{t}} \cdot \nabla' [\frac{G_{1}}{\varepsilon_{1}} - \frac{G_{2}}{\varepsilon_{2}}] dr + \int_{S} E_{t}(\mathbf{r}') \hat{\mathbf{t}} \cdot \hat{\mathbf{e}}_{z} \times \nabla' [G_{1} - G_{2}] dr',$$

(6)

in which  $\hat{\mathbf{t}} = \hat{\mathbf{n}} \times \hat{\mathbf{e}}_z$  is the tangential unit vector at the surface. Eq. (6) contains three coupled surface integral equations of Fredholm second kind that govern  $E_z$ ,  $B_n$ , and  $H_t$  at the boundary surface. Their form is similar to the coupled surface integral equations derived for TM mode (containing  $H_z$ ,  $D_n$ , and  $E_t$ ) in [7] and [8] but with interchanged role of  $\varepsilon$  and  $\eta$ . Such coupled integral equations do not have, in general, analytical solutions and should be numerically solved.

(4)

### **III.NUMERICAL SOLUTION**

In order to solve the coupled integral equations in Eq. (6), the simplest trapezoidal integration scheme is used. First, the boundary is divided into N segments. At each segment there are three unknown fields, namely,  $E_z$ ,  $B_n$  and  $H_t$ which are related to each other through coupled integrals in Eq. (6). The discretized form of Eq. (6) is constructed as:

$$E_{z}(p) = E_{z}^{i}(p) - \sum_{q=1}^{N} a(p,q) E_{z}(q) + \sum_{q=1}^{N} b(p,q) H_{i}(q),$$

$$B_{n}(p) = B_{n}^{i}(p) + \sum_{q=1}^{N} c(p,q) E_{z}(q) + \sum_{q=1}^{N} d(p,q) B_{n}(q) + \sum_{q=1}^{N} e(p,q) H_{i}(q),$$

$$H_{i}(p) = H_{i}^{i}(p) + \sum_{q=1}^{N} f(p,q) E_{z}(q) + \sum_{q=1}^{N} g(p,q) B_{n}(q) + \sum_{q=1}^{N} g(p,q) B_{n}(q) + \sum_{q=1}^{N} g(p,q) H_{i}(q),$$
(7)

where p and q are  $p^{th}$  and  $q^{th}$  segments of the boundary, respectively. The functions a(p,q) to h(p,q) are coefficients of the unknown fields and can easily be derived from Eq. (6) as:

$$a(p,q) = -\hat{\mathbf{n}}(q) \cdot \nabla_{\mathbf{q}} \left[ G_{1}(p,q) - G_{2}(p,q) \right] \Delta l_{q},$$
  

$$b(p,q) = i \omega \left[ \mu_{1}G_{1}(p,q) - \mu_{2}G_{2}(p,q) \right] \Delta l_{q},$$
  

$$c(p,q) = i \omega \left[ \mu_{1}\varepsilon_{1}G_{1}(p,q) - \mu_{2}\varepsilon_{2}G_{2}(p,q) \right] \hat{\mathbf{n}}(p) \cdot \hat{\mathbf{t}}(q) \Delta l_{q},$$
  

$$d(p,q) = -\hat{\mathbf{n}}(p) \cdot \nabla_{\mathbf{q}} \left[ G_{1}(p,q) - G_{2}(p,q) \right] \Delta l_{q},$$
  

$$e(p,q) = \hat{\mathbf{n}}(p) \cdot \hat{\mathbf{e}}_{\mathbf{z}} \times \nabla_{\mathbf{q}} \left[ \varepsilon_{1}G_{1}(p,q) - \varepsilon_{2}G_{2}(p,q) \right] \Delta l_{q},$$
  

$$f(p,q) = i \omega \left[ \varepsilon_{1}G_{1}(p,q) - \varepsilon_{2}G_{2}(p,q) \right] \hat{\mathbf{t}}(p) \cdot \hat{\mathbf{t}}(q) \Delta l_{q},$$
  

$$g(p,q) = -\hat{\mathbf{t}}(p) \cdot \nabla_{\mathbf{q}} \left[ \frac{G_{1}(p,q)}{\varepsilon_{1}} - \frac{G_{2}(p,q)}{\varepsilon_{2}} \right] \Delta l_{q},$$
  

$$h(p,q) = \hat{\mathbf{t}}(p) \cdot \hat{\mathbf{e}}_{\mathbf{z}} \times \nabla_{\mathbf{q}} \left[ G_{1}(p,q) - G_{2}(p,q) \right] \Delta l_{q}.$$
  
(8)

with  $\Delta l_q$  as the length of the  $q^{th}$  segment. All of the above coefficients are well-defined for  $p\neq q$ . However, denominator of the Green's functions and their derivatives vanish for p=qcase which will be problematic. Using the trick of Cauchy principal value shows that all the coefficients vanish at limits  $q \rightarrow p$  and  $\Delta l_q \rightarrow 0$  except for b(p,q) and f(p,q). They are determined to have the following limits:

$$\begin{split} &\lim_{q \to p} b(p,q) = \\ &i\omega \big[ \mu_1 G_1(p,p+1) - \mu_2 G_2(p,p+1) \big] \Delta l_p, \\ &\lim_{q \to p} f(p,q) = \\ &i\omega \big[ \varepsilon_1 G_1(p,p+1) - \varepsilon_2 G_2(p,p+1) \big] \hat{\mathbf{t}}(p) \cdot \hat{\mathbf{t}}(p+1) \Delta l_p, \end{split}$$
(9)

With these coefficients in hand, the Eq. (7) yields three non-homogenous linear algebraic equations for each segment. Consequently, for N segments there are 3N non-homogenous equations with 3N unknowns. They can be solved simply by matrix algebra. Using the found fields at the boundary, the other field values within the nanowire and surrounding medium can be calculated through Eqs. (1) and (2), respectively. Integral equations in Eqs. (1) and (2) are normal and can be implemented easily by a simple trapezoidal scheme with no need to Cauchy principal value or other tricks.

To do the calculations, a massive computer code was developed by the authors. All of the mentioned procedures including boundary discretization, coefficients evaluation, matrix manipulation and field computation are automatically done by the code. In the following subsections two examples are presented.

## A. Interaction with an ordinary dielectric nanowire

A simple dielectric nanowire (here a glass) with circular cross-section of radius R=400 nm and with  $\varepsilon_2$ =2.25  $\varepsilon_0$  and  $\mu_2$ = $\mu_0$  is considered. The nanowire is placed in the vacuum and is illuminated by a TE-polarized plane wave with wavelength  $\lambda$ =400 nm. The interaction of light with the nanowire is simulated by the mentioned code. A square region of side length 800 nm with the nanowire in its center is considered as the computational space and is divided into differential squares of side length 5 nm. The nanowire boundary is discretized

into N=500 segments. Simulated distribution of  $E_z^2$  is shown in Fig. 2a for a typical time.

Fig. 2a clearly shows that in this interaction, the incident light is refracted with a smaller wavelength within the wire (because  $\varepsilon_2 > \varepsilon_1$ ) and transmits (forward-scattered) through it. The transmitted light is focused in a point within the vacuum confirming the fact that it acts as a cylindrical lens. A portion of the light is also reflected (back-scattered) from the nanowire and interferes with the incident filed and constructs an interference pattern.



Fig. 2: Contour plot of simulated  $E_z^2$  in scattering of a plane TE polarized light from a glass nanowire, a. The three-dimensional plot of such distribution, b.

#### **B.** Interaction with a plasmonic nanowire

In this subsection, a silver nanowire with circular cross-section of radius R=400 nm is considered. The nanowire is placed in the vacuum and is interacted by a TE polarized

light with  $\lambda$ =400 nm. The electromagnetic constants of silver in  $\lambda$ =400 nm, as reported in [7], are  $\varepsilon_2 = \varepsilon_0$  (-4.22+i0.73) and  $\mu_2 = \mu_0$ , respectively. In this wavelength, silver is a plasmonic material and can support surface plasmon wave under interaction with a TM polarized light.



Fig. 3: Contour plot of the simulated  $E_z^2$  in scattering of a plane TE polarized light from a plasmonic nanowire, a, and its three dimensional plot, c. The same plots for scattering of a TM polarized light from a plasmonic nanowire, b and d.

The simulated distribution of  $E_z^2$  in contour and three-dimensional plots is shown in Figs. 3a and 3c, respectively. It is seen that no electric field penetrates into the nanowire. This is due to the imaginary part of  $\varepsilon_2$  representing a kind of loss mechanism. The transmitted light is vanishingly zero but the reflected one is significant; confirming the fact that silver is a good reflector of light.



Fig. 4: Contour plots of the field distribution in scattering of a plane TE-polarized light from a plasmonic nanowire for  $\lambda >> R$ , a, for  $\lambda \approx 2R$ , b, and for  $\lambda << R$ , c.

In the surface region, there is no sign of surface plasmon excitation and propagation. If the incident light was in TM mode rather than in TE, then surface plasmon would be excited and propagate at the surface. This mode was also calculated by the code and its results are plotted in Figs. 3b and 3d showing the propagation excitation and of surface plasmons. The figures show that, excitation of propagating surface plasmon by TM mode can guide the incident light to the dark back region of the wire and lighten there, but, there is no such thing in the TE mode. More details of TM mode scattering can be found in [7] and [8].

Field distributions for very large wavelengths  $(\lambda >> R)$ , for moderate wavelengths  $(\lambda \approx 2R)$ , and very small wavelengths ( $\lambda \leq R$ ) are calculated by the code and plotted in Figs. 4a, 4b and 4c, respectively. At  $\lambda >> R$  extreme, which is the electrostatic limit, the electric field penetrates through the whole of nanowire. In this limit there is no sign of reflected and transmitted light and also no dark region (shadow) behind it. For  $\lambda \approx 2R$  case a pattern which contains spatial distribution of minima and maxima is formed. The pattern is in fact the familiar light diffraction from the wire. A shadow-like dark region is being constructed in its back. For the other extreme  $\lambda << R$ , the incident light on the wire is completely reflected from the wire and the geometrical shadow is formed behind it.

#### **IV.DISCUSSION**

Simulation of light scattering from a glass nanowire correctly shows light reflection, refraction with a smaller wavelength, transmission and also its concentration in a focus which reminds that it is a cylindrical lens. In geometrical optics the focal length of a thick lens in air is calculated from [11]:

$$\frac{1}{f} = (n_1 - 1) \left( \frac{1}{R_1} - \frac{1}{R_2} + \frac{(n_1 - 1)d}{n_1 R_1 R_2} \right)$$
(10)

where  $n_1$  is the lens refractive index,  $R_1$  and  $R_2$  are curvature radii of left and right surfaces of the lens, respectively, and d is the lens

thickness. For the cylindrical scatterer of Fig. 2, which is in fact a thick glass lens, the focal point is calculated to be 600 nm on the right of the wire center. Its position is shown by a small star in Fig. 2. This position is different from the simulated focus shown by a small point in the figure. The origin of the difference is the fact that the Eq. (10) is derived in geometrical optics (i.e. short wavelengths compared to the lens size) by paraxial approximation. In the Stratton-Chu integral equations mentioned above such no approximations were applied and the results are exact.

In the scattering of the TE light from a plasmonic nanowire no sign of plasmon excitation and propagation is seen. It is different from the TM light scattering in which surface plasmon is excitable. Surface plasmon is an electronic wave that can be excited in material surfaces by incident light whenever two necessary conditions are satisfied [12]. The first condition is that the real part of electric permittivity of the material ( $\varepsilon_{2r}$ ) must have different sign from that of the surrounding medium  $(\varepsilon_{1r}).$ The second condition is that there must be a normal component of electric field on the surface. In the scattering of TE light from silver nanowire the first condition is satisfied. However, as the electric field of TE mode is parallel with the wire axis it does not have normal component on the nanowire surface and so the second condition in not satisfied.

Light scattering with decreasing wavelengths shows that the electrostatic, diffraction and geometrical optics regions appear in turn. This result is discussable from two aspects. Firstly, for very long wavelengths (compared to scatterer size), no scattering will occur and the incident light will propagate unperturbedly. In fact, small objects will not scatter longwavelength lights, or in other words, a longwavelength light cannot see small objects. Secondly, if wavelength of the incident light is comparable to size of the scatterer then diffraction occurs. Diffraction is a direct result of wave-like nature of the light. By decreasing the wavelength of the incident light the diffraction level also decreases. In fact, the geometrical optics is the sort-wavelength limit of the wave optics with zero diffraction and with distinct shadow regions.

## V. CONCLUSION

In this paper, three coupled surface integral equations governing the scattering of a monochromatic TE polarized light from a nanowire were derived. The simulation results for different nanowires and their physical interpretation show that the derived equations are correct and powerful. Extension to the scattering of a TE polychromatic light is considered as the future work of the authors.

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#### SCOPE

Original contributions relating to advances, or state-of-the-art capabilities in the theory, design, applications, fabrication, performance, and characterization of: Lasers and optical devices; Laser Spectroscopy; Lightwave communication systems and subsystems; Nanophotonics; Nonlinear Optics; Optical Based Measurements; Optical Fiber and waveguide technologies; Optical Imaging; Optical Materials; Optical Signal Processing; Photonic crystals; and Quantum optics, and any other related topics are welcomed.

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