ABSTRACT— We present a novel slanted faces of thin-disk composite Yb:YAG \ YAG laser which is side-pumped by four non-symmetric hollow-ducts. The pump light distribution in the disk is modeled by using Monte-Carlo ray tracing method. The temperature distribution inside the crystal is calculated by taking into account either the concentration of Yb$^{3+}$ ion or the different transmission of laser output coupler. By using Finite Element Analysis (FEA) method, we calculated the absorption efficiency through the disk. The resonator is simulated by self consistently method. The resulting of optical efficiency and the output power of our laser have been modeled.

KEYWORDS: Edged-pumped thin disk laser, Monte-Carlo ray tracing, optical to optical efficiency.

I. INTRODUCTION

According to several advantages of Yb:YAG crystal, It has been a promising candidate for high – power laser diode – pumped solid state laser [1, 2]. High average power have been obtained with high efficiency by using different laser cavity configurations, such as end-pumped microchip lasers, edge-pumped and side- pumped laser systems [3-6]. The main disadvantage of ytterbium-doped material is their quasi three-level nature caused by the thermal population of terminated lasing level [7]. This effect becomes worse at high temperature induced from the heat generated by the absorbed pump power inside the Yb:YAG crystal. The thermal conductivity of Yb:YAG crystal decreases and the thermal loading parameter increases with increasing ytterbium concentration . In addition, there is strong emission quenching, which is attributed to uncontrolled impurities during crystal growth. These concentration dependent thermal properties of Yb:YAG have great unwanted effects on the laser performance of side – pumped Yb:YAG disk laser. The thermal conductivity, thermal expansion coefficient and thermal loading of Yb:YAG crystals related to the temperature. The temperature increment which is induced by the pump power deposited on the gain medium is critical factor to be considered in the laser performance of side-pumped Yb:YAG high power disk laser. Some numerical and analytical calculations of ytterbium concentration in side – pumped slab geometry have been affected by Eggleston et al. [8], and Kane et al. [9]. Also, Rutherford et al. gave an analytic description of edged-pumped quasi – three level slab laser based on the assumption of the laser material’s temperature-independent absorption coefficient [10]. The work by Rutherford et al. [10] presented a compromise between pump absorption efficiency and uniformity as a function of the product of the absorption coefficient and the slab width. In addition, Chen et al. explored a method of using gradient doping concentration to optimize the pumping efficiency and the pumping uniformity in edged- and end pumped slab lasers , separately [11, 12]. Dong et al. reported on the effect of Yb$^{3+}$-ion concentration on the performance of end – pumped Yb:YAG microchip lasers at ambient temperature [13]. Dong et al. have demonstrated the lower the Yb concentration, the better on the lasing of YAG crystal with different dopant at high pump power level.
In Ref. [13], a 1-mm-thick Yb:YAG crystal with 10 At. % Yb$^{3+}$ ion of microchip laser at ambient temperature is described. Different output powers and crystal structures such as microchip composite [14] and ceramic microchip [15] lasers have been reported for efficient edged-pumped thin disk laser. In Ref. [15], Taira et al. presented a square composite microchip with an un-doped cap layer surrounding the core material for better heat conduction. Recently, the new geometry of side-pumped thin disk laser is presented by our group [16]. The structure of the gain medium which are side-pumped slanted sides with an un-doped cap on the active medium are applied to achieve high output power and obtain better efficiency in our delivery system. In this work, temperature-dependent and temperature-independent absorption coefficients are presented. Then, the related consequence of output power due to different transmission of output coupler and different concentration of Yb$^{3+}$-ions calculated.

II. PROCESS OF THE WORK

In this work, the side-pumped slanted faces disk laser was carried out with a 0.2-mm-thick Yb:YAG crystal doped with 5, 10, 15, and 20 At. % Yb$^{3+}$ ions as a gain medium. Also, a 1.3-mm-thick YAG crystal bonded on the gain medium and has a role of un-doped cap to reduce the ASE effect in the gain medium. In the manner of edged-pumped of this specific shape of disk laser, we used four non-symmetric hollow-ducts [16]. The schematic diagram of the set up illustrated in Fig. 1(a). The bottom surface of the disk is highly-reflection-coated at both 941 nm and 1030 nm to act as a rear mirror of the cavity. A concave-plane mirror was used as output coupler with different transmissions (T_OC) of 3, and 10% at 1030 nm.

The overall cavity length was 400 mm in linear setup as shown in Fig. 1(b). Four high power stacked LD in 941 nm with output divergence about 0.25° and 10° of fast axis and slow axis respectively were used as the pump sources. About 96% of the total pumping power is incident on the Yb:YAG crystal after passing through the non-symmetric hollow-ducts.

The numerical simulation which is used for our CW-operation of the thin disk laser consists of four distinct steps [17]. The first step is to calculate the distribution of absorbed pump power within the crystal. This is done by using Monte-Carlo-ray tracing method. We taking into account the changes of absorption efficiency with crystal temperature and population inversion of the system. The second step is to calculate the temperature within the crystal that results from energy conversion loss between pump and laser energy. In the third and fourth steps the population inversion and the output power are calculated respectively. Assuming by an ideal plane-parallel and infinitesimal short resonator, the last two steps have been calculated. We should to notice that, steps one through three are iterated until a steady state is reached.
III. Numerical Simulation of the CW-Operation of the Thin Disk Laser

The distribution of absorbed pump energy within the crystal is calculated by means of Monte-Carlo-ray tracing. This means that the path of randomly generated pump photons is followed through the optical system regarding the absorption as a statistical process. We used 10000 random photons for each pump source.

It means that every photon starts with a random position on the entrance slanted facets of the non-symmetrical hollow ducts. A random moving direction which is determined following the calculated angle distribution of a hollow duct which is determined according to an assumed Gaussian profile with the spectral width of the diodes. The path of the photon is then followed through the crystal until it is absorbed completely. Remaining of the photons regards to the geometry of the gain medium are trapped on the internal front slanted surface of the gain medium and again reabsorbed in returning direction through the disk. Then, the absorbed photons are counted in elements of a mesh into which the crystal is divided. In our modeling a mesh consists of 13 layers perpendicular to the crystal axis (z-axis), 110 squares in length direction (X-axis) and the same meshing for width direction (Y-direction) of the gain medium. We used typically triangular meshing structure in slanted facets of the gain medium for doing realistic simulation of the disk. In order to determine whether a passing photon is absorbed, its way through the crystal is divided into two or more steps. For each step the transmission in axial direction is calculated at Cartesian position of the photon. If the photon is absorbed, which is determined by generation of a random number, the exact position of absorption is found by further comparison of the random number with transmission after some of the mesh elements in that step [16], Fig. 2.

In Sub-section (A), we used the absorption coefficient in order to obtain the pump light distribution inside the crystal and in Sub-section (B), we have done the simulation with the temperature dependent absorption coefficient.

A. Pumping distribution with constant absorption coefficient

Related to the specific structure of the gain medium, we have done geometrical optics calculations and applied them into a ray tracing method with concentration based on the goal of the uniformity of the pump light distribution inside the gain medium. In our simulation, we supposed that, the pump light has a Gaussian spectral distribution. Also, the absorbed pump power density with the constant absorption coefficient is as a function of the position along the width of the disk.

The absorbed pump power density distribution inside the disk with constant absorption coefficient is depicted in Fig. 3. As in Fig. 3(a) shows, regarding the effect of pump absorption saturation, fewer pumps light are absorbed at the near entrance faces of the disk compare to the center of the disk. In addition, in Fig. 3(b), it is clear that the absorbed pump power density profile in X-direction and Y-direction are similar to each other and have a Gaussian profile and have a peak around the center of the disk and its value in both X- and Y-direction are 287 W/mm^3. Furthermore, we
illustrated the 3D irradiance profile of the pump light distribution inside the disk in Fig. 3(a).

Regarding the propagation trace of the photons through the disk and also the overlapping of the rays which are reached from four hollow ducts, one could see this effect as a deep in the irradiance profile.

B. Pumping distribution with the crystal temperature dependent absorption coefficient

Since in section A, we restricted to the case of constant absorption coefficient and do not apply to our model with the temperature-dependent absorption coefficient, we have done it in this section. The calculation of crystal temperature as a function of the absorbed energy distribution usually is symmetric around the crystal axis. So, the calculation of temperature is done for the axial symmetry. In our simulation, the generated heat due to the quantum defect of 8.56% is taken from the calculated average absorption distribution. It is applied to the elements of a two-dimensional mesh. The resulting heat flow between every pair of neighboring elements is determined and the temperature is adjusted until the heat flow is reduced underneath a certain error limit. The heat conductivity $\lambda$ is taken to be temperature dependent [18]:

$$
\lambda(T) = \lambda_0 \frac{T_0 - T_{\text{off}}}{T - T_{\text{off}}}
$$

With the heat conductivity $\lambda_0 = 13.0 \text{W/mK}$ at $T_0 = 300 \text{K}$ and $T_{\text{off}} = 42 \text{K}$. The influence of the heat sink geometry is described by the value of its heat resistance. This value depends on the pump beam radius and is determined by using the finite-element-model (FEM) method on a model of the crystal and the heat sink. The final calculation of temperature distribution through the disk is illustrated in Fig. 4. Because of the axial symmetric of temperature distribution in four sides of the slanted edged pumped disk laser, we depicted a quarter of the gain medium via the whole thickness of the disk.

The absorption coefficient $\alpha$ can be expressed as:

$$
\alpha = \alpha_0 \frac{1}{1 + (I_0/I_{\text{sat}})}
$$
where $\alpha_0$ is the small-signal absorption coefficient, $I_0$ and $I_{sat}$ are the pump intensity and the Yb:YAG laser saturation intensity (at 941 nm), respectively ($I_{sat} = h\nu/\sigma\tau$), where $h\nu$ is the photon energy, $\sigma$ is the stimulated emission cross section, and $\tau$ is the excited manifold storage lifetime.

The absorbed pump power distribution is calculated by Finite Element Analysis (FEA). The wavelength of pump light set at 941 nm with Gaussian spectral distribution. The calculated results are shown in Fig. 5. As shown in Fig. 5, introduction of the temperature-dependent absorption coefficient causes the non-uniform distribution of the pump power density along the width of the gain medium. It makes the calculation of heat deposit distribution from pump power more accurate. On the other hand, we consider the dopant concentration as the variable in 10, 15, 20% of Yb$^{3+}$ ion in our calculation. So, the absorbed pump power density profile on the X-Y planes is relatively uniform.

In the following section, we used the results of previous section, in order to calculate the laser output power due to two concepts: First with different transmission of output coupler and second with different concentration of Yb$^{3+}$ ion.

**IV. LASER OUTPUT POWER CALCULATION AND OPTICAL EFFICIENCY OF THE DISK**

**A. Different transmission of output coupler**

Based on the work reported by Beach [20] and Rutherford et al. [10], we calculate the output power of an edged-pumped quasi-three level thin disk laser. Besides the effects of lower manifold depletion, output coupling, temperature-dependent thermal conductivity and pump absorption saturation our particular structure of the gain medium consider to the thermal effects of the laser output power [21]. The considered case is of multiple transverse mode oscillation, where the laser mode nearly fills the disk.

The data stands for our configuration which are used as the basis of our calculations are given in Table 1. [19]; [20].

Therefore, the laser output power can be written as a function of the pump power as given by [20].

$$P_{out} = \eta_{\text{slope}} (\eta_{\text{abs}} P_p - P_0)$$  \hspace{1cm} (4)

where, $P_{out}$ is the laser output power, $P_p$ is the pump power, $\eta_{\text{slope}}$ is the slope factor, $\eta_{\text{abs}}$ is the pump efficiency and $P_0$ is the threshold factor. The terms of $\eta_{\text{slope}}$, $\eta_{\text{abs}}$ and $P_0$ are given in [22]. The expression of $P_{out}$ as referred to (6), shows the temperature dependence of three parameters: Boltzmann
population fractions \( f_a, f_b, f'_a, f'_b \), stimulated emission cross section \( \sigma_e \) and absorption coefficient \( \sigma_{\text{abs}} \).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Crystal thickness (doped-region)</td>
<td>200 (μm)</td>
</tr>
<tr>
<td>Cap thickness (undoped-region)</td>
<td>1.3 (mm)</td>
</tr>
<tr>
<td>Dopant concentration (C_{Yb})</td>
<td>5, 10, 15, 20 (%)</td>
</tr>
<tr>
<td>Number of non-symmetric hollow-duct</td>
<td>4 (pics)</td>
</tr>
<tr>
<td>Pump Wavelength ( (\lambda_p) )</td>
<td>941 (nm)</td>
</tr>
<tr>
<td>Number of Pump beam pass</td>
<td>16</td>
</tr>
<tr>
<td>Temperature of cooling fluid ( (T_c) )</td>
<td>286 (K)</td>
</tr>
<tr>
<td>Fluorescence lifetime [20]</td>
<td>950 (μs)</td>
</tr>
<tr>
<td>Heat conductivity ( (\lambda, \text{@} 300K) )</td>
<td>13.0 (Wm(^{-1})K(^{-1}))</td>
</tr>
<tr>
<td>Reflectivity of output coupler ( (R) )</td>
<td>3, 5, 10, 15 (%)</td>
</tr>
<tr>
<td>Resonator internal losses ( (L) )</td>
<td>~ 0.2 %</td>
</tr>
<tr>
<td>Linear expansion coefficient [21]</td>
<td>6.9 × 10(^{-6})</td>
</tr>
<tr>
<td>Crystal thickness (doped-region)</td>
<td>200 (μm)</td>
</tr>
<tr>
<td>Cap thickness (undoped-region)</td>
<td>1.3 (mm)</td>
</tr>
<tr>
<td>Dopant concentration (C_{Yb})</td>
<td>5, 10, 15, 20 (%)</td>
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</tr>
<tr>
<td>Pump Wavelength ( (\lambda_p) )</td>
<td>941 (nm)</td>
</tr>
</tbody>
</table>

The Boltzmann occupation factors of pump and laser levels depending on the temperature are expressed as follows [22]:

\[
\begin{align*}
    f_a &= \frac{\exp\left(-\frac{E_a^b}{KT}\right)}{\sum \exp\left(-\frac{E_i}{KT}\right)}, \quad f_b = \frac{\exp\left(-\frac{E_b^l}{KT}\right)}{\sum \exp\left(-\frac{E_i}{KT}\right)} \\
    f'_a &= \frac{\exp\left(-\frac{E_a^p}{KT}\right)}{\sum \exp\left(-\frac{E_i}{KT}\right)}, \quad f'_b = \frac{\exp\left(-\frac{E_b^p}{KT}\right)}{\sum \exp\left(-\frac{E_i}{KT}\right)}
\end{align*}
\]

where the sums are done over all the Stark levels of the ground manifold, and

where, the sums are shown over all Stark levels of the excited manifold. \( E_a^p \) and \( E_b^p \) are energies for the lower and the upper pump Stark levels, \( E_a^l \) and \( E_b^l \) are energies for the lower and the upper laser Stark levels, respectively. \( K \) is the Boltzmann constant, \( E_i \) is the energy for each Stark level of the ground manifold and \( E_j \) is the energy for each Stark level of the exited manifold.

The temperature dependence of \( \sigma_e \) for Yb:YAG has been given by Chen et al. [12].

The output power of Yb:YAG disk laser as a function of the absorbed pump power for T_{oc} = 3, 5, 10, 15% is shown in Fig. 6. For the case of C_{Yb} = 5%, the transmission of output coupler (T_{oc}) are 2, 3, 4 and 5% due to the absorbed pump power thresholds of 0.2 – mm – thick disk laser. The absorbed pump power threshold of 0.2-mm-thick Yb:YAG laser is
183 W for 20 atomic % of ytterbium concentration.

As shown in Fig. 6, the output power increase linearly with the absorbed pump power when the pump power is well above the pump power threshold for Yb:YAG crystal doped with 10, 15, and 20 At. % Yb$^{3+}$. This effect is respect to the nature of quasi-three level operating scheme. Also, high efficiency can be achieved by using high pump power intensity. There is a drop of the slope efficiency for 10 At. % Yb:YAG thin disk laser, which is caused by the low transmission of output coupler. For 15, 20 At. % Yb:YAG, the output power increase linearly with absorbed pump power when the absorbed pump power is lower than 183 W and 231 W for T_{oc}= 3%, respectively. In Fig. 6(a), the highest slope efficiency (with respect to the absorbed pump power) of 24% was achieved by using T_{oc}= 2% for C_{Yb} = 5 At. %.

We obtained the output power by increasing one-step of output coupler transmissions from 2% to 5%. In Fig. 6(b), we calculate the output power for C_{Yb}=10 At. %, due to different transmission of output coupler.

Table 2 Performance of Yb:YAG side-pumped slanted – faces disk laser with different Yb$^{3+}$ dopant. \( \lambda \)l , laser emitting wavelength ; \( P_a \) , Power threshold ; \( P_{as} \) , Absorbed pump power ; \( P_{out} \) , Maximum output power ; \( \eta_{slope} \) , Maximum optical – to – optical slope efficiency corresponding to absorbed pump power.

<table>
<thead>
<tr>
<th>Yb:YAG</th>
<th>( T_{oc} ) (%)</th>
<th>( \lambda )l (nm)</th>
<th>( P_a ) (W)</th>
<th>( P_{as} ) (W)</th>
<th>( P_{out} ) (W)</th>
<th>( \eta_{slope} ) (%)</th>
<th>( \eta_{O-O(a)} ) (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>5 At.%, 0.2 mm-thick</td>
<td>2</td>
<td>1030</td>
<td>504</td>
<td>673.3</td>
<td>158</td>
<td>24</td>
<td>40</td>
</tr>
<tr>
<td>10 At.%, 0.2 mm-thick</td>
<td>3</td>
<td>1030</td>
<td>538</td>
<td>673.3</td>
<td>138</td>
<td>20</td>
<td>40</td>
</tr>
<tr>
<td>15 At.%, 0.2 mm-thick</td>
<td>4</td>
<td>1030</td>
<td>605</td>
<td>673.3</td>
<td>117</td>
<td>17</td>
<td>40</td>
</tr>
<tr>
<td>20 At.%, 0.2 mm-thick</td>
<td>5</td>
<td>1030</td>
<td>673</td>
<td>673.3</td>
<td>75</td>
<td>11</td>
<td>40</td>
</tr>
</tbody>
</table>

Also, we obtained the highest slop efficiency of 21% by using \( T_{oc}= 5 \)%. For this case the optical – to – optical slope efficiency is 53%. By increase of Yb$^{3+}$ concentrations to 15%, we obtained the output power of 288 W with slope efficiency (respect to the absorbed pump power) of 25% and the optical – to – optical slope efficiency of 63% Fig. 6(c). In Fig. 6(d), we used 20% of Yb$^{3+}$ concentrations due to different output coupler transmission for 3, 5, 10, 15 % respectively. The highest output power were obtained 296 W with the optical – to – optical slope efficiency of 67% and the slope efficiency with respect to the absorbed pump power of 24%. The output power and slope efficiency (with respect to the absorbed pump power) with different At.% of Yb$^{3+}$ ions concentration are also listed in Table 2.

B. Different concentration of Yb$^{3+}$ ion

The output power calculation respect to the absorbed pump power in different of Yb$^{3+}$ ion concentration of C_{Yb} = 10, 15 and 20 At. % have been done. We use different transmission of output coupler of 3, 10 and 15 At. %, respectively. The results of the output power calculation are illustrated in Fig. 7(a, b, c). As shown in Fig. 7(a), the highest output power is obtained for C_{Yb} = 20 At. % for T_{oc} = 15% with the slop efficiency of 10%. In Fig. 7(b), the output power calculation due to the transmission of the output coupler (10%) in different concentration of Yb$^{3+}$ ion is depicted. we obtained the highest output power for the C_{Yb} = 20 At. %. However, by use of C_{Yb} = 15 At. % the output power calculation is near to the use of C_{Yb} = 20 At. %. The slope efficiency (respect to the absorbed pump power) of 31% and optical – to – optical slope efficiency of 75% were obtained. By decreasing the output coupler transmission into 3%, we calculated the output power. The results is depicted in Fig. 7(b). As shown in Fig. 7 (c), for T_{oc} = 3% the output power of C_{Yb} = 15 and 20 At. % were calculated whereby we show that there are nearly similar to each other. The optical – to – optical slope efficiency of 54% and the slope efficiency (respect to the absorbed pump power) of 30% have been obtained. By comparing the results in Fig. 7(a, b, c), the output power threshold has been decreased for C_{Yb} = 20 At. % from 640 W to 197 W corresponding to the decrease of output.
coupler transmission from $T_{oc} = 15\%$ to $T_{oc} = 3\%$.

![Graph](image1)

![Graph](image2)

![Graph](image3)

**Fig. 7.** The output power of Yb:YAG/YAG disk laser as a function of the absorbed pump power for Yb:YAG crystals doped with different Yb$^{3+}$ concentrations in thickness of 0.2 mm. (A) $T_{oc} = 3\%$, (B) $T_{oc} = 10\%$, (C) $T_{oc} = 15\%$.

**V. CONCLUSION**

In this paper, we present a side-pumped slanted faces of high power Yb:YAG/YAG thin disk laser which is pumped by the manner of non-symmetric hollow ducts. Distribution of pump light and absorbed pump power in the active medium are calculated by the use of Monte-Carlo ray tracing and Finite Element Analysis (FEA) methods, respectively. By using the results of FEA, the output power of the gain medium is calculated in two following steps: First, respect to the different value of the output coupler transmission and second with different concentration of Yb$^{3+}$ ion. For those two steps we solved the rate equation for three-level lasing medium. Finally, by comparing the results one can understand from the table the slope efficiency of the side pumped slanted faces Yb:YAG/YAG high power thin disk laser.

**ACKNOWLEDGMENTS**

The authors of this paper would like to express their fully thanks to the collaborations of I. Mashaiekhky Asl and M. Esmaeili in INLC during the preparation of this work.

**REFERENCES**


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