Plasmonic Solar Cells, a New Way to Enhance Energy Conversion Efficiency: Analysis and Modeling of Effect of Metal Geometry

Farshad Farhadnia*, Ali Rostami, and Samieh Matloub
Faculty of Electrical and Computer Engineering, University of Tabriz, Tabriz, Iran
*Corresponding author Email: farhadnia@tabrizu.ac.ir

Received: Jun. 13, 2018, Revised: Apr. 8, 2018, Accepted: May. 5, 2018, Available Online: June. 30, 2019
DOI: 10.29252/ijop.13.1.61

ABSTRACT—In this article, the effect of plasmonic properties of metal nanoparticles with different shapes, and moreover, their plasmonic-photonic interaction, on solar cell performance were investigated and simulated. Because of low conversion efficiency and then high cost of solar cells, it is difficult to commercialize and replace them with conventional energy resources. But in recent years, the plasmonic solar cell has been very popular. In this study, it is shown that the enhancement of near-field electromagnetic waves severely affects the generation rate, which handles the carrier’s generation in the solar cell equations and causes alteration of the photocurrent. This means that by manipulating the plasmonic properties of nanoparticles (shape and density) and their interaction with photons in solar cell structure, distribution of electromagnetic fields will be altered. Hence, the optical power related to the poynting vector is changed. So, with the aim of improving the solar cell some important parameters such as alteration of nanoparticle shape and their inter-distance were investigated. Finally, a comparison between traditional solar cells and our improved structure was undertaken.

KEYWORDS: Plasmonic, Nanoparticles, Plasmonic-photonic interaction, Solar cell

I. INTRODUCTION

Photovoltaic (PV) technology, which involves the direct conversion of sunlight into electric energy, is one of the components of an evolving energy mix. Several attractive features of this technology include pollution-free operation, relatively low costs and modularity. In the future, solar cells may well play an increasingly prominent role in global electricity generation in order to limit environmental pollution and to slow down the rise of greenhouse gas concentration [1-5]. As a simple model, a semiconductor solar cell is based on a simple p-n junction. A qualitative description of cell performance can be given in terms of a simple model based on the Shockley diode equation in the dark and under illumination. This model is sufficient for understanding the basic carrier transport mechanisms in the cell, and roughly for predicting the performance parameters of a solar cell. Most of the traditional solar cells are based on silicon because of its stability, non-toxicity, well-developed technology and abundance in nature. However, a major limitation of the thin-film solar cells is poor absorption of light, compared to the wafer-based solar cells [6-10]. It is well established that light-trapping by increasing its optical path length inside the absorbing film, for obtaining high efficiency, is crucial for thin-film solar cells. In light of the above restriction, a new method using plasmonic structures can improve the absorption of light, due to excitation of localized surface plasmon. Noble metals such as silver (Ag), gold (Au), aluminium (Al) and copper (Cu), support surface plasmon due to their free-electron-like behavior. Surface plasmon is the collective oscillations of excited free electrons of metallic particles. This unique property of metallic nanoparticles (NPs) can be used to
enhance the optical absorption of solar cells through scattering of light and near-field concentration of light [11-17]. The contribution of these mechanisms depends on the nanoparticle material, shape, and size, and the refractive index of the surrounding dielectric. In this work, we used the plasmonic-based NPs to enhance the traditional solar cell specification. It is shown that the near-field electromagnetic wave severely affects generation rate, which handles the carrier generation in the solar cell equations. This means that by manipulation of plasmonic properties of the NPs in the solar cells structure, the distribution of electromagnetic fields can be altered. Hence, the optical power and generation rate related to the Poynting vector is changed, which can influence directly solar cell output parameters. So, for improving the solar cell critical parameters, the alteration of NPs shapes and inter-distance were done. Finally, the comparison between traditional solar cell and our improved structure was performed. Finally it should be noted that all of the simulations in this work were done by COMSOL 4.4 and MATLAB.

II. BACKGROUND AND THEORY

A few equations describe the behavior of charge carriers in semiconductors under the influence of an electromagnetic field; all of which cause deviations from thermal equilibrium conditions. These equations are called the basic equations for semiconductor device. The Poisson equation relates the static electric field to the space-charge density [2-4]:

$$\frac{d^2 \varphi(x)}{dx^2} = -\frac{d\varepsilon(x)}{dx} = \frac{\rho(x)}{\varepsilon_0 \varepsilon_s}$$  \hspace{1cm} (1)$$

where $\varphi$, $\varepsilon_0$, and $\varepsilon_s$ are the electrostatic potential, the permittivity of free space and the static relative permittivity of the medium, respectively. Based on our study, the electron current density ($J_e$) and the hole current density ($J_h$) are given by [2]:

$$J_e(x) = +qD_e \frac{dn(x)}{dx} + q\mu_e n(x) \varepsilon(x) \hspace{1cm} (2)$$

$$J_h(x) = +qD_h \frac{dp(x)}{dx} + q\mu_h p(x) \varepsilon(x) \hspace{1cm} (3)$$

where $n$, $p$, $\mu_e$, $\mu_h$, $D_e$, and $D_h$ are electron and hole densities, the electron and hole mobility, and the electron and hole diffusion constants, respectively. It is notable that the first terms on the right hand side of Eqs. 2 and 3 are diffusion currents driven by a concentration gradient, and the second terms are drift currents driven by the electric field. Indeed, the latter case will be manipulated by nanoparticles’ (NPs) or nanorods’ (NRs) Plasmonic radiation. It means that by the use of NPs/NRs, electromagnetic distribution in the different sections of p-n junction will be altered, so the drift currents driven by the electric field. Indeed, the latter case will be manipulated by nanoparticles’ (NPs) Plasmonic field. It means that by the use of NPs, electromagnetic distribution in the different sections of p-n junction will be altered, so the drift currents driven by the electric field can be changed. Also, by changing the NPs’ materials, shape, geometry and inter-distance between them, the electric field distribution can be easily manipulated. In the following formula, divergence of the current density, $J$, is contributed to recombination and generation rates of charge carriers by the continuity equation. Electron and hole continuity equations may be written as [2]:

$$\frac{1}{q} \frac{dJ_e(x)}{dx} - r_e(x) + G_e(x) = 0 \hspace{1cm} (4)$$

$$\frac{1}{q} \frac{dJ_h(x)}{dx} - r_h(x) + G_h(x) = 0 \hspace{1cm} (5)$$

In these equations $r(x)$ and $G(x)$ are the position-dependent volume recombination and photo-generation rates, respectively. Finally, by substituting Eqs. 2 and 3 into the continuity Eqs. 4 and 5, a couple set of transport equations are driven as [2]:

$$D \frac{d^2 n}{dx^2} + \mu_e \frac{dn}{dx} + n \mu_e \frac{d\varepsilon}{dx} - r_e(x) + G_e(x) = 0 \hspace{1cm} (6)$$
Electron and hole transport equations, Eqs. 6 and 7, are coupled with the electric field E. The coupled set of differential equations can be solved with different degrees of accuracy. It is important to note that for improving the solar cells’ specification, in this work we used NPs Plasmonic properties, which influence the original electric field in near-field state. In other words, the original field in the solar cell structure can be perturbed by NPs Plasmonic in near-field. For extra and effective manipulation, an array of NPs was used. It is known that because of the interaction between NPs Plasmonics, non-uniform electromagnetic fields are arisen in solar cell’s different areas, which contribute to optical power and optical generation rate. Actually, optical generation rate as an important parameter in the solar cell system, contributes to the time averaged Poynting vector, which is given by [6]:

\[ G_{ave} = \eta_{opt} \frac{-\nabla \cdot S_{ave}}{h \nu} \]  

(8)

where, \( \eta_{opt} \), \( S_{ave} \), \( \nu \) are optical quantum yield, time averaged Poynting vector, Planck constant and incidence frequency, respectively. The time averaged Poynting vector has been considered as the radiant flux around any NPs and calculated by ExH*. The optical generation rate in Eq. 8 can be substituted in Eqs. 4 and 5 and electron and hole continuity equations can be re-written by this alteration. Indeed, by manipulating optical generation rate in Eq. 8, the solar cell’s key parameters such as photon current can be changed. The traditional solar cell photon current can be illustrated as [18, 19]:

\[ I_{ph} = I_{ph_s} + k_c (T_c - T_s) \frac{G}{G_{ref}} \]  

(9)

where \( I_{ph_s} \), \( k_c \), \( T_c \), and \( T_s \) are solar cell current under standard condition, temperature coefficient of short circuit current, solar cell operating temperature and reference temperature, respectively. Moreover, \( G \) and \( G_{ref} \) attribute to the intensity of irradiance in solar cell and reference intensity, about \( 10^3 \) Watts/m\(^2\), respectively. As a result of that \( G \) includes the incidence irradiances (\( G_{inc} \)) as well as intensity generated by the NPs near-field Plasmonic field (\( G_{pl} \)). It should be noted that after calculating solar cell photo-current, the solar cell open circuit voltage and short circuit current can be obtained, which are given by [18, 19]:

\[ V_{oc} = \frac{AKT}{q} \ln \left( \frac{I_{ph}}{I_0} \right) \]  

(10)

\[ I = I_{ph} - I_{sh} \exp \left[ \frac{q(V + IR_c)}{AKT} - 1 \right] \left( \frac{V + IR_c}{R_{oh}} \right) \]  

(11)

where \( A, K, \) and \( q \) are the diode ideality factor, Boltzmann’s constant and electron charge, respectively. Moreover, \( I_0 \) relates to the current dependency on temperature and short circuit current. This means that by manipulating Poynting vector in the Plasmonic condition, solar cell’s key parameters such as optical generation rate and solar cell photon current are remarkably changed. For this, in this study, we investigated the NPs optical properties’ manipulating effect on generation rate and optical power, and Poynting vector was considered as the critical factor for this study. At last, the solar cell’s \( I-V \) (current-voltage) relations, which depend on \( I_{ph} \) and its original factors such as NPs Plasmonic field intensity, are introduced by:

\[ V = \frac{AKT}{q} \ln \left( \frac{I_{ph} - I_0}{I_0} - 1 \right) + IR_c \]  

(12)

In these equations, \( R_s \) and \( R_{oh} \) are the solar cell series and shunt resistors, respectively. Therefore, with knowledge about this point, the NPs Plasmonic field intensity has effectively influenced the photon current and solar cell output voltage and current; we can design a solar cell based on NPs for engineering the solar cell photon current.

### III. RESULTS AND DISCUSSION

In this section, the simulation results in the case of the 2-D simple structure solar cell are illustrated. Based on Eqs. 8-13, which emphasize the plasmonic effect of optical power and optical generation rate on solar cell photon current and its influence on output current and voltage, we can compare four different structures with traditional structures.
Actually, the original aim was to manipulate the photon current based on optical power and optical generation rate engineering, which can dramatically affect solar cell fill factor and its other important parameters. In fact, by manipulating the NPs’ optical properties, we can try to alter the solar cell fill factor.

Figure 1a shows the traditional simple p-n structure without any NPs. In terms of this case, the interaction of light with different wavelengths was simulated by COMSOL; its results are illustrated in Figs. 1(b), (c), and (d). In these figures we show the I-V curve, photo-current, and fill factor versus different wavelengths, respectively. In Fig. 1(b), this shows the I-V curve for different wavelengths, in which the maximum current for the traditional structure is about 0.2 A. We tried to improve this case by manipulating the plasmonic-photonic interaction. The photo-current alteration versus wavelength is illustrated in Fig. 1(c); its average is about 0.12 A. Finally, the solar cell fill factor for traditional structure is shown in Fig. 1(d).

It is easily seen that its change is based on photo-current alteration. The alteration of parameters relates to the interaction of light with the solar cell at different wavelengths. We can manipulate the penetration of light into the solar cell structure to change light intensity for extra manipulation of the solar cell photo-current based on equation 9. In other words, in this equation we can manage the intensity radiation with regard to the plasmonic feature. Some simulations about the penetration of light into the traditional solar cell at different wavelengths are illustrated in Fig. 2.
It seems that in these structures the plasmonic-photonic interaction can manipulate the light intensity into the solar cell, and consequently the related photo-current can be dramatically improved. It should be noted that the original aim was to manipulate the interaction of light with the solar cell structure, which was done by changing the NPs’ morphology. With changes such as size and type and as well as medium materials, the plasmonic features are altered. It contributes to the plasmonic engineering or plasmonic hybridization [20, 21]. Additionally, plasmonic-photonic interaction can be considered. In fact, by engineering the latter case, non-uniformity will be controlled, which affects the solar cell parameters. By these selections, improved parameters such as the related I-V curves, photo-current, and the distribution of intensity into the solar cell are presented. Initially, we started with photo-current for four different structures illustrated in Fig. 3, which is shown in Fig. 4. In Fig. 4(a) the average of current is about 0.14 A and for Fig. 4(b) it is about 0.21 A; for fig. 4c it is smaller than 0.1 A, and finally, for Fig. 4(d) it is about 0.17 A.

The average data can be compared with the traditional case in Fig. 1c. It is shown that the photo-current is improved in the case of Figs. 4(a), (b), and (d). It contributes to the plasmonic-photonic interaction and producing field non-uniformity by NPs. Indeed, the NPs’ plasmonic coupling to the far-field causes more light trajectories inside of the solar cell; and this clearly leads to the high absorption by carriers based on Eq. 9. In fact, the transport equations will be manipulated by the NPs’ plasmonic effect on carrier generation in Eqs. 6 and 7. Particularly, in Fig. 4(b) the maximum amount of photo-current occurred; and moreover, a good profile was attained for Fig. 4(a). In this structure the optimum level of the NPs’ plasmonic field can be coupled to the far-field region, which causes the maximum effect on the carrier generation. By interaction of the chain of plasmonic NPs with an incidence electromagnetic wave, the NPs plasmonic field interacts with the photonic mode of chain (geometry). This interaction creates the lattice plasmon which is due to the constructive interference of the NPs’ field. So, at any point in space, we can calculate the NPs’ field interference which is the main reason to coupling to far-field. By the way, the lattice plasmon optical properties are severely limited due to the photonic mode and geometry. This restriction defines at which wavelengths the constructive interference can be occurred [22-23]. We just need to manipulate the field non-uniformity inside the solar cell, by the NPs’ plasmonic field and its interaction with...
photonic structure, to affect the carrier generation rate. It should be noted that the noisy behavior in this figure relates to the numerical approximation. Actually, due to using the finest mesh by COMSOL for the highest accuracy and link to MATLAB for I-V curve analyzing, we could not use a continuous form of wavelengths between 400 nm and 900 nm. This means that we have to use some important wavelengths; so the discontinuity or noisy behavior in this figure is inevitable. In the following, the related I-V curves are presented in Fig. 5.

Fig. 5. I-V curves for different structures at different wavelengths from 400 nm to 950 nm. a) and c) for spherical NPs and b) and d) for tri-angular NPs

Due to the best characteristics of photo-current in Figs. 4(a) and (b), we focused on exploring these structures and compared them with other cases. The modeling results show that the current in Fig. 5(b) reaches 0.35 A and is more effective than the traditional case in Fig. 1(b). The I-V curves are derived from Eqs. 11 and 12. We used the well-known iterative Newton-Raphson method to find the coupled equation roots. It was found that the calculated current for the improved structures was severely influenced by the NPs' effect and as well by the light incidence wavelength. Actually, the NPs' plasmonic effect and the non-uniformity produced by them inside of the solar cell, for instance in Fig. 5(b), have a dramatic effect on output current. Based on these data, the fill factor simulations are illustrated in Fig. 6.

Fig. 6. Fill-factor curves for different structures at different wavelengths from visible to NIR wavelengths. a) and c) for spherical NPs and b) and d) for tri-angular NPs

Fig. 7. Spherical NPs plasmonic effect on propagation of light in solar cell structure: a) 537 nm, b) 653 nm, c) 785 nm, and d) 854 nm.

The alteration in this figure is based on the related photo-current in Fig. 4 for each structure; so with regard to this parameter, the maximum efficiency can occur for structure 3(b). Consequently, the major reason for this end will be presented. We thought by manipulation of the intensity distribution in the solar cell structure, its critical parameters such as photo-current and fill factor could be managed. In other words, the NPs' plasmonic field coupling to the far-field or the field non-uniformity created by this phenomenon has a severe effect on carrier generation and output.
current. Then by altering the field non-uniformity, the passing of the light into the solar cell is increased, which leads to enhancing of the photon absorption by carriers. We modeled the interaction of light with spherical NPs and moreover with two coupled tri-angular NPs to change the interaction of light with matter, which is illustrated at different wavelengths, for instance in Figs. 7 and 8.

It is notable that the original aim was to explore the plasmonic generated by Au NPs and its photonic interaction in the far-field region. This means that by changing the morphology structure such as NPs’ inter-distance, the plasmonic-photonic interaction can be altered. Also, the optimum NPs’ inter-distance was selected. Moreover, the plasmonic-plasmonic interaction between two closed tri-angular NPs was investigated, and it can be concluded that the more efficient manipulation of light interaction with matter occurred for this structure, which is shown in Fig. 8. Furthermore, in Figs. 7 and 8, the effect of different wavelengths was investigated. In these figures, it is notable to mention the plasmonic-photonic coupling effect on light penetration into the solar cell. By this effect the non-uniform electric field is produced in the solar cell, which is unlike the traditional solar cell, and this is the main reason to create the high-efficiency solar cell system. Finally as an important result, it can be mentioned that by using the NPs with different morphology, 1) the light absorption by the new structure is increased; and 2) the field distribution (non-uniformity and its amplitude) into the solar cell is changed. These factors relate to the NPs’ plasmonic features and the plasmonic-photonic coupling properties, and by changing these factors the solar cell efficiency can be altered.

**IV. CONCLUSION**

In this study, it was shown that the NPs generating near-field electromagnetic waves severely affected optical power, which handles the carrier generation in the solar cell equations. In other words, by manipulating plasmonic properties of NPs (shape and density) and their effect on photons in solar cell structure, distribution of electromagnetic fields in solar cells is altered. By manipulation of these factors the solar cell’s critical parameters such as I-V curve, photo-current, and fill factor improved. The simulation results showed that for improving the fill factor or I-V curves, as the important parameters in solar cells, the alteration of morphology and NPs’ inter-distance are necessary.

**REFERENCES**


Ali Rostami received the Ph.D. degree in Electrical and Computer Engineering from Amirkabir University of Technology, Tehran, Iran in 1998. He is currently a professor of Faculty of Electrical and Computer Engineering, Photonics and Nano crystal Research Lab, University of Tabriz, Iran. He has worked on the research fields of Nano photonics, Opt mechatronics, Plasmonics, Photonic Crystals (Modeling and Optical VLSI), Optical Processing and Computing and etc.

Samieh Matloub received her Ph.D. in photonic/electronic engineering from University of Tabriz, Tabriz, Iran, in 2010. She is currently Assistant professor of electronic engineering and photonics science at the University of Tabriz. Her teaching and research interests include optoelectronic devices and optical integrated circuits.
THIS PAGE IS INTENTIONALLY LEFT BLANK.