

# Numerical Analysis of Mushroom-type Traveling Wave Electro-absorption Modulators Using Full-Vectorial Finite Difference Method

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**Abstract**— Larger width of P-cladding layer in p-i-n waveguide of traveling wave electro-absorption modulator (TWEAM) results in lower resistance and microwave propagation loss which provides an enhanced high speed electro-optical response. In this paper, a full-vectorial finite-difference-based optical mode solver is presented to analyze mushroom-type TWEAM for the first time. In this analysis, the discontinuities of the normal components of the electric field across abrupt dielectric interfaces which are known as the limitations of scalar and semivectorial approximation methods are considered. The optical field distributions in mushroom-type TWEAM and conventional ridge-type TWEAM of the same active region for 1.55  $\mu\text{m}$  operation are presented. The important parameters in the high-frequency TWEAM design such as optical effective index which defines optical velocity and transverse mode confinement factor are calculated. The modulation response of mushroom-type TWEAM is calculated by considering interaction of microwave and optical fields in waveguide and compared to that of conventional ridge-type TWEAM. The calculated 3dB bandwidths for ridge-type and mushroom-type TWEAM are about 139 GHz and 166 GHz for 200  $\mu\text{m}$  and 114 GHz and 126 GHz for 300  $\mu\text{m}$  waveguide length, respectively.

**KEYWORDS:** Full-vectorial finite difference method (FV-FDM), Traveling wave modulator, Electro-absorption, Mushroom-type TWEAM.

## I. INTRODUCTION

High-speed and high-efficiency electro-absorption modulators (EAM) are key devices for microwave analog fiber links as well as high-data-rate optical wavelength division

multiplexing systems and high-speed optical time division multiplexing systems. Broadband and high-electrical-to-optical efficiency are two main criteria in the design of EAM. Toward the high performance in the EAM application, traveling-wave (TW) structure is one of candidates to overcome the conventional RC-lump limitation. Therefore, the waveguide can be made long to enhance the extinction ratio and high modulation efficiency without losing its high-speed performance [1-5]. However, in practical, the limitation of TWEAM in p-i-n layers is generally restricted by the high microwave propagation loss because of the metal skin effect, highly-loaded capacitance and the high resistance in p-layer [6]. Increasing the width of p-cladding layer with the same i-layer for reduction of the p-i-n waveguide resistance can improve the microwave propagation loss and thus the high-speed electro-optical response [7].

The optical waveguide defines the intrinsic cross-sectional geometry of the TWEAM. The waveguide core region is the absorption region of the modulator, which from the electrical point of view presents the depletion layer of a hetero-junction pin-structure. Therefore, electrical, optical, and electro-optical designs are interlocked. The optical wave is guided by the index guiding layers formed by the active layer (absorption region) together with upper and lower cladding layers. The thickness of the active layer determines the electric field strength for a given applied voltage. The value of the field dependent absorption coefficient inside this material is subject to its bandgap compared to the photon energy

[8].

The optical effective index defines the optical velocity, which is an important parameter in the high-frequency TWEAM design. Transverse mode confinement factor is also very important since only the confined fraction of the optical mode within the active region can be modulated.

Accurate calculation of modal fields, optical effective index and confinement factor for optical waveguide of TWEAM is perhaps the most basic and indispensable for designing TWEAM. Various numerical techniques, e.g., finite difference method (FDM) [9, 10], finite element method (FEM) [11], imaginary distance beam propagation method (ID-BPM) [12], and mapped Galerkin method (MGM) [13], have been proposed to perform this task. Among them, the FDM is an attractive candidate because of the simplicity of its implementation and the sparsity of its resulting matrix.

The early application of the FDM was based on the scalar wave equation which is valid only for the optical waveguides with very small refractive index difference (weakly guiding approximation). In recent years, the FDM has been employed to determine semivectorial guided modes where the polarization dependence is taken into account [14]. Yet the polarization coupling is ignored. More recently, the FDM has been applied for analyzing the full vectorial modes for the optical waveguides with large refractive index differences in regions of high field intensity [15].

In this paper, a full-vectorial finite-difference-based optical mode solver is used to analyze mushroom-type traveling wave electro-absorption modulator for the first time. The discontinuities are considered in FDM, and full-vectorial distributions of the modal fields can be generated for mushroom-type and ridge-type traveling wave electro-absorption modulators. Three adjacent grid points are used to approximate each differential operator, so the solution is more accurate than that obtained by using two adjacent grid points. The optical effective index and transverse mode confinement factor for mushroom-type and

ridge-type TWEAMs are calculated and compared. Then, the modulation response of mushroom-type TWEAM is calculated by considering interaction between microwave and optical fields in waveguide and compared with conventional ridge-type TWEAM.

## II. THEORY AND ANALYSIS

### A. Full-vectorial Wave Equation

The full-vector eigenvalue equation based on electric fields can be derived from the Maxwell's equations. In a source free region, and assuming a periodic time variation,  $e^{j\omega t}$ , we have:

$$\nabla \times \underline{\mathbf{E}} = -jk\eta_0 \underline{\mathbf{H}} \quad , \quad \nabla \times \underline{\mathbf{H}} = jk \frac{1}{\eta_0} n^2 \underline{\mathbf{E}} \quad (1)$$

$$\nabla \cdot (n^2 \underline{\mathbf{E}}) = 0 \quad , \quad \nabla \cdot \underline{\mathbf{H}} = 0 \quad (2)$$

where  $\underline{\mathbf{E}}$  and  $\underline{\mathbf{H}}$  are the electric and magnetic field vectors,  $k$  and  $\eta_0$  are the free-space wave vector and wave impedance, respectively.  $n=n(x,y)$  is the refractive index of the guiding medium. Through a simple derivation [16], we have the following full-vectorial wave equation for the electric field:

$$\nabla^2 \underline{\mathbf{E}} + \nabla \left( \frac{1}{n^2} \nabla (n^2) \cdot \underline{\mathbf{E}} \right) + n^2 k^2 \underline{\mathbf{E}} = 0 \quad (3)$$

Only two components of the electric field are required. If the transverse components  $e_x$  and  $e_y$  are known, the longitudinal component may be calculated by:

$$\nabla \cdot (n^2 \underline{\mathbf{E}}) = 0 \quad (4)$$

for the case that refractive index profile of an optical waveguide does not vary along the propagation direction. Therefore, it makes sense to separate the electric field into transverse and longitudinal components, and assume  $z$ -dependence of  $e^{-j\beta z}$ .

$$\underline{\mathbf{E}}(x, y, z) = (\mathbf{e}_t + \hat{z}e_z) e^{-j\beta z} \quad (5)$$

where  $\beta = k_0 n_{o\_eff}$  is the propagation constant and  $n_{o\_eff}$  is the effective index. The full-vector wave equation can be written in terms of the transverse components,

$$\nabla^2 \mathbf{e}_t + \nabla \left( \frac{1}{n^2} \nabla (n^2) \cdot \mathbf{e}_t \right) + n^2 k^2 \mathbf{e}_t = \beta^2 \mathbf{e}_t \quad (6)$$

The longitudinal component  $e_z$  can be computed from  $\mathbf{e}_t$  using the divergence relation:

$$j\beta e_z = \nabla \cdot \mathbf{e}_t + \frac{1}{n^2} \nabla (n^2) \cdot \mathbf{e}_t \quad (7)$$

Equation (6) can be written in terms of the two transverse field components  $e_x$  and  $e_y$  as:

$$\begin{bmatrix} P_{xx} & P_{xy} \\ P_{yx} & P_{yy} \end{bmatrix} \begin{bmatrix} e_x \\ e_y \end{bmatrix} = \beta^2 \begin{bmatrix} e_x \\ e_y \end{bmatrix} \quad (8)$$

where the differential operators are defined as:

$$P_{xx} e_x = \frac{\partial}{\partial x} \left[ \frac{1}{n^2} \frac{\partial (n^2 e_x)}{\partial x} \right] + \frac{\partial^2 e_x}{\partial y^2} + n^2 k^2 e_x \quad (9)$$

$$P_{yy} e_y = \frac{\partial^2 e_y}{\partial x^2} + \frac{\partial}{\partial y} \left[ \frac{1}{n^2} \frac{\partial (n^2 e_y)}{\partial y} \right] + n^2 k^2 e_y \quad (10)$$

$$P_{xy} e_y = \frac{\partial}{\partial x} \left[ \frac{1}{n^2} \frac{\partial (n^2 e_y)}{\partial y} \right] - \frac{\partial^2 e_y}{\partial x \partial y} \quad (11)$$

$$P_{yx} e_x = \frac{\partial}{\partial y} \left[ \frac{1}{n^2} \frac{\partial (n^2 e_x)}{\partial x} \right] - \frac{\partial^2 e_x}{\partial y \partial x} \quad (12)$$

Equation (8) is a full-vectorial eigenvalue equation which describes the modes of propagation for an optical waveguide. The two coupled transverse field components  $e_x$  and  $e_y$  taken together are the eigen functions, and the corresponding eigenvalue is  $\beta^2$ . The non-zero diagonal terms  $P_{xy}$  and  $P_{yx}$  reveal that the two field components  $e_x$  and  $e_y$  are coupled, that is, the eigenvalue equation cannot be divided into two independent eigenvalue equations to be solved separately for  $e_x$  and  $e_y$ . Because of this coupling, the eigen modes of an optical waveguide are usually not purely TE or TM in nature. Nevertheless, often one of the two transverse field components is much larger than the other, and the mode can be treated as quasi TE or TM.

## B. OPTICAL WAVEGUIDE STRUCTURE FOR TWEAM AND FINITE DIFFERENCE SCHEME

The p-i(MQW)-n structure of the mushroom-type electro-absorption waveguide modulator

is shown schematically in Fig. 1. The optical waveguide is described by a refractive index profile  $n(x,y)$ . The refractive index profile has been broken up into small rectangular elements or pixels, of size  $\Delta x \times \Delta y$ . Over each of these elements, the refractive index is constant. Thus, discontinuities in the refractive index profile occur only at the boundaries between adjacent pixels. Because the index profile is symmetric about the y-axis, only half of the waveguide needs to be included in the computational domain.

The finite-difference grid points, i.e., the discrete points at which the fields are sampled, are located at the center of each cell. The general situation for an arbitrary grid point P with its neighboring points N, S, W, E, NW, NE, SW, and SE is illustrated in Fig. 2. The refractive indices for these points are labeled here as  $n_P, n_N, n_S, n_W, n_E, n_{NW}, n_{NE}, n_{SW}$ , and  $n_{SE}$ , respectively.

Now we convert the partial differential Eq. (8) into a corresponding finite difference equation. We first deal with the differential operator  $P_{xy}$  which operates on  $e_x$ . Because  $e_x$  is continuous across horizontal interfaces, the  $\partial^2 e_x / \partial y^2$  term may be approximated with the simple three point difference, that is,

$$\left. \frac{\partial^2 e_x}{\partial y^2} \right|_P \approx \frac{1}{(\Delta y)^2} (e_x^N - 2e_x^P + e_x^S) \quad (13)$$

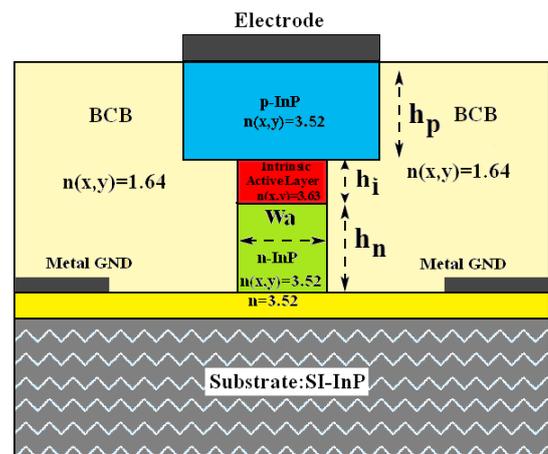


Fig. 1 Schematic structure of mushroom traveling-wave electro-absorption modulator.

However, when there is an index discontinuity between W and P or between P and E, the finite difference equations must be

modified to account for the discontinuity in  $e_x$ . One of the most straightforward techniques for deriving finite difference approximations is the Lagrange interpolation.

NW •	N *	NE •
W *	P ×	E *
SW •	S *	SE •

**Fig. 2** Labeling scheme used for the finite difference model.

The Lagrange interpolation is simply the lowest order polynomial which goes through all of the sample points. The derivatives can then be easily computed from the polynomial coefficients of the interpolating function.

To accomplish this, we use a modified interpolation procedure in which we fit the points  $e_{xW}$ ,  $e_{xP}$  and  $e_{xE}$  with a piecewise quadratic polynomial function ( $e_x$ ) as:

$$\phi(x) = \begin{cases} A_W + Bx + Cx^2 & \text{in cell W} \\ A_P + Bx + Cx^2 & \text{in cell P} \\ A_E + Bx + Cx^2 & \text{in cell E} \end{cases} \quad (14)$$

The function  $\phi(x)$  is satisfied with the following conditions:

$$\begin{aligned} e_{xW} &= A_W - B\Delta x + C(\Delta x)^2 \\ e_{xP} &= A_P \\ e_{xE} &= A_E + B\Delta x + C(\Delta x)^2 \end{aligned} \quad (15)$$

Considering that  $n^2 e_x$  to be continuous at  $x = \pm \Delta x/2$ , that is,

$$\begin{aligned} n_W^2 \left\{ A_W - \frac{1}{2} B\Delta x + \frac{1}{4} C(\Delta x)^2 \right\} &= n_P^2 \left\{ A_P - \frac{1}{2} B\Delta x + \frac{1}{4} C(\Delta x)^2 \right\} \\ n_P^2 \left\{ A_P - \frac{1}{2} B\Delta x + \frac{1}{4} C(\Delta x)^2 \right\} &= n_E^2 \left\{ A_E - \frac{1}{2} B\Delta x + \frac{1}{4} C(\Delta x)^2 \right\} \end{aligned} \quad (16)$$

Equations (15) and (16) together give five linear equations which can be solved for the five unknown polynomial coefficients. After summarizing the results, we have

$$\begin{aligned} P_{xx}e_x|_P &= \frac{1}{(\Delta x)^2} (\alpha_W e_x^W - 2\alpha_P e_x^P + \alpha_E e_x^E) + \\ &\frac{1}{(\Delta y)^2} (e_x^N - 2e_x^P + e_x^S) + k_P^2 n_P^2 \end{aligned} \quad (17)$$

where the constant  $\alpha_W$ ,  $\alpha_P$  and  $\alpha_E$  are dimensionless ratios defined by:

$$\begin{aligned} \alpha_W &\equiv \frac{4 \left( n_W^2 n_P^2 + n_E^2 n_W^2 \right)}{n_P^2 + 2n_E^2 n_P^2 + 2n_W^2 n_P^2 + 3n_E^2 n_W^2} \\ \alpha_P &\equiv \frac{2 \left( 2n_P^2 + n_W^2 n_P^2 + n_E^2 n_P^2 \right)}{n_P^2 + 2n_E^2 n_P^2 + 2n_W^2 n_P^2 + 3n_E^2 n_W^2} \\ \alpha_E &\equiv \frac{4 \left( n_E^2 n_P^2 + n_E^2 n_W^2 \right)}{n_P^2 + 2n_E^2 n_P^2 + 2n_W^2 n_P^2 + 3n_E^2 n_W^2} \end{aligned} \quad (18)$$

A similar procedure can also be used to derive the finite difference equations for  $p_{yy}e_y$ ,  $p_{xy}e_y$  and  $p_{yx}e_x$ . Then (7) is converted into a standard matrix eigenvalue equation.

This developed finite difference approximation can be applied even in the presence of abrupt dielectric interfaces where the field is discontinuous. The technique described here involves fitting a piecewise-quadratic polynomial to three adjacent grid points.

### III. TWEAM FREQUENCY RESPONSE

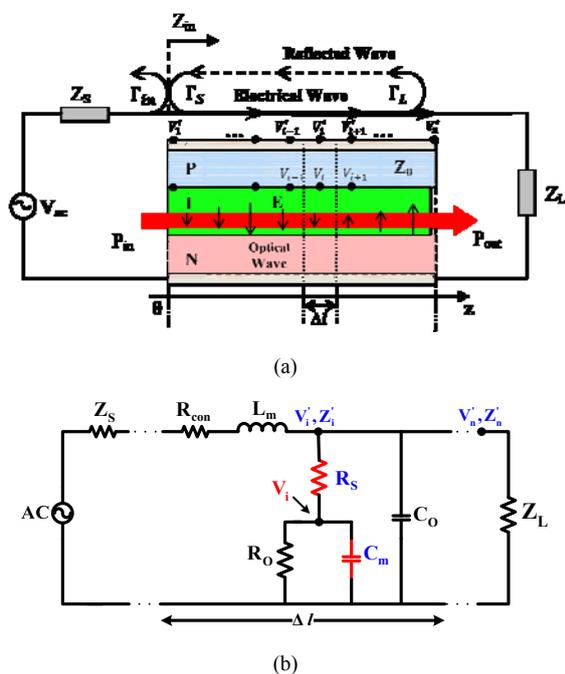
TWEAMs are devices to modulate light waves corresponding to traveling electric fields along the electrode consisting of a transmission line. Because the absorption coefficient of TWEAMs depends on the electric voltage, the modulation of optical wave occurs by the absorption change due to modulated electric signals. Fig. 3 shows the principle of operation and circuit model for a unit length of TWEAM transmission line [17, 3].

The circuit model contains the conduction resistance  $R_{con}$ , the inductance  $L_m$ , the vertical series resistance  $R_s$ , the junction capacitance  $C_m$ , an outer parasitic capacitance  $C_o$ , and a differential resistance  $R_o$  parallel to  $C_m$  which is caused by photo-generation of carriers in the intrinsic layer. The effect of junction resistance  $R_o$  becomes significant only at high incident optical power.

The small signal frequency response for TWEAM can be obtained as follows [4,3]:

$$|P_{ac}|^2 = \left| \sum_{i=1}^n \left( V_i e^{j \frac{\omega}{c_0} n_{o\_eff} (i-1) \Delta l} \right) \right|^2 \quad (19)$$

where  $V_i$  is the modulating voltage in  $i$  section. The calculation of the small signal modulation response requires the knowledge of the optical index  $n_{o\_eff}$  and the circuit model elements for calculation of  $V_i$ . The circuit elements can easily be extracted from the TWEAM transmission line microwave properties  $Z_0$  (characteristic impedance) and  $\gamma$  (propagation constant) [18], which are obtained via full-wave simulations of the given geometry.



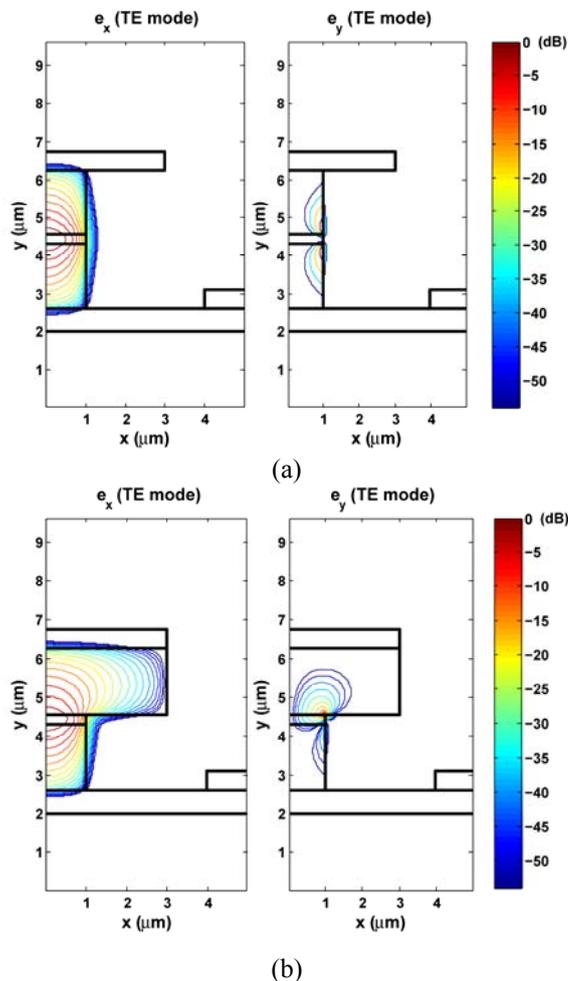
**Fig. 3** (a) Principle of operation, and (b) circuit model for a unit length of TWEAM transmission line.

#### IV. RESULTS AND DISCUSSIONS

In this section, we use the full-vectorial finite difference optical mode solver to calculate the fundamental effective index and transverse mode confinement factor of a mushroom-type and traveling wave electro-absorption modulator.

The main material parameters in order to perform waveguide simulations are the refractive indices. The waveguide simulation considers 2-dimensional structures. The active region with thickness  $h_i$  is composed of MQW.

The thickness of the active layer is considered to be  $0.2 \mu\text{m}$ . In order to improve the junction capacitance, we use a small intrinsic buffer layer on top of the active layer with thickness of  $0.2 \mu\text{m}$  [4]. The width of the active layer ( $W_a$ ) is taken as  $2 \mu\text{m}$  and simulation is carried out for the wavelength of  $1.55 \mu\text{m}$ .



**Fig. 4** Transverse electric field components  $e_x$  and  $e_y$  for the fundamental quasi TE mode (a) ridge-type TWEAM, (b) mushroom-type TWEAM.

Figure 4 depicts the waveguides cross-section and the calculated TE field contour of ridge-type and mushroom-type waveguides for  $e_x$  and  $e_y$ . As mentioned before, the  $e_x$  transverse field component is much larger than the  $e_y$  component and the mode is treated as quasi TE.

The effective index defines the optical speed, which should be known in the design of a traveling wave modulator. After computing modal eigenvalue  $\beta_2$  of traveling wave electro-absorption modulator, by solving (6), the effective index can be calculated as follows.

$$n_{o\_eff} = \frac{\beta}{k_0} \tag{20}$$

Figure 5 shows the calculated effective index of mushroom-type and ridge-type structures for fundamental mode of TE polarization.

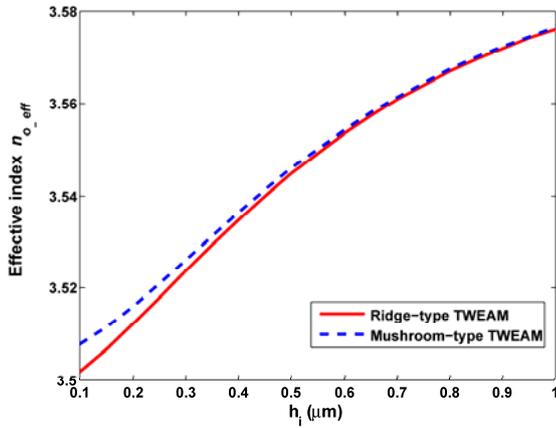


Fig. 5 Optical effective index for fundamental mode vs. active region thickness.

Figure 6 shows the optical confinement factor as a function of the active region thickness. 0.2 μm of MQW thickness yields an optical confinement factor of %19.1 for mushroom-type and %21.6 for ridge-type TWEAM. This is due to better confinement of the electric field in the intrinsic region of ridge-type compared to that of mushroom-type.

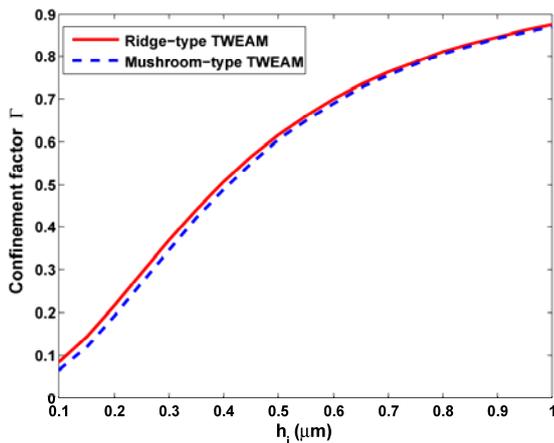


Fig. 6 Optical confinement factor vs. active region thickness

Typical values for the active region thickness are 0.2 to 0.5 μm [5].

Figure 7 shows the calculated microwave loss for mushroom-type and ridge-type TWEAM using finite element method. As the p-cladding layer width increases, the microwave loss decreases.

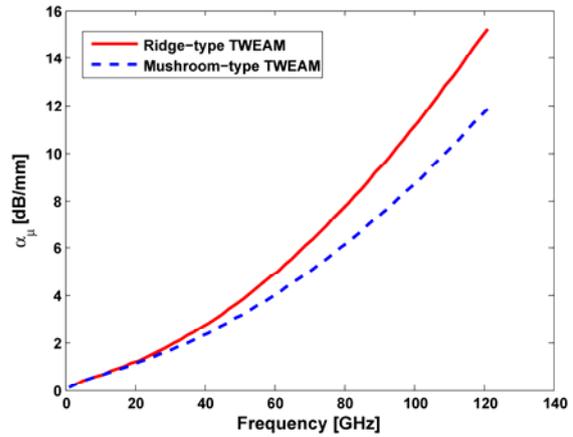


Fig. 7 Microwave loss vs. frequency.

The variation of microwave loss vs. P-layer width is illustrated in Fig. 8. In this analysis, the microwave frequency is assumed to be 80 GHz. As shown in the figure, increasing P-layer width leads to decrease microwave loss. As the P-layer width is increased the junction capacitance C<sub>m</sub> increases because of the higher parasitic capacitance as shown in Fig. 9.

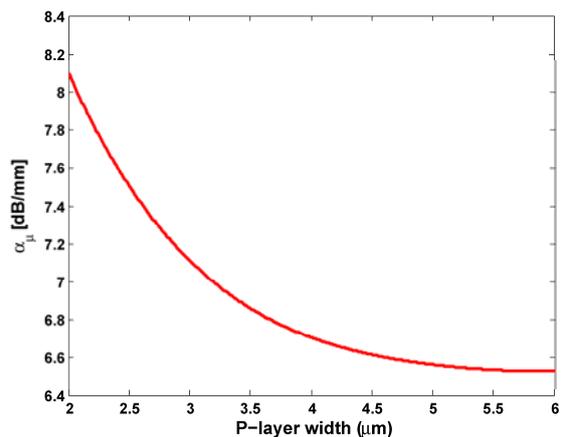


Fig. 8 Microwave loss vs. p-layer width.

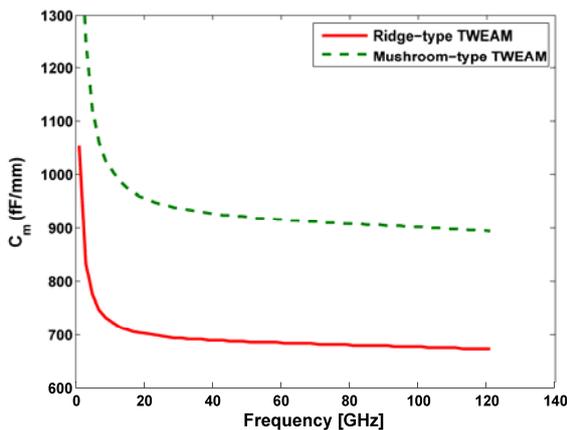


Fig. 9 Junction capacitance vs. frequency.

Figures 10 and 11 show the real parts of the characteristic impedance and microwave refractive index. As the p-cladding layer width increases, the microwave velocity and characteristic impedance of waveguide decrease due to increased junction capacitance in waveguide.

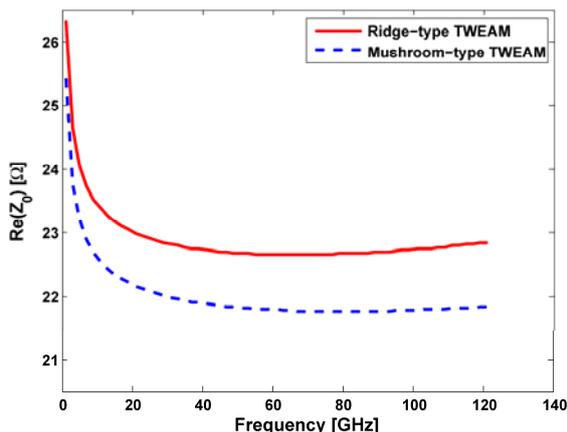


Fig. 10 Real part of characteristic impedance vs. frequency.

Figure 12 shows the calculated frequency response for mushroom-type and ridge-type TWEAM with different lengths and  $Z_L=25 \Omega$ . In this case, all the waveguide parameters are the same. The overall waveguide loss and velocity mismatch increase as the device length increases. The microwave loss and velocity mismatch reflect the decrease in optical modulation, as shown in the plot. The 3dB bandwidths for ridge-type and mushroom-type TWEAM are about 139 GHz and 166 GHz for 200  $\mu\text{m}$  and 114 GHz and 126 GHz for 300  $\mu\text{m}$  waveguide length, respectively.

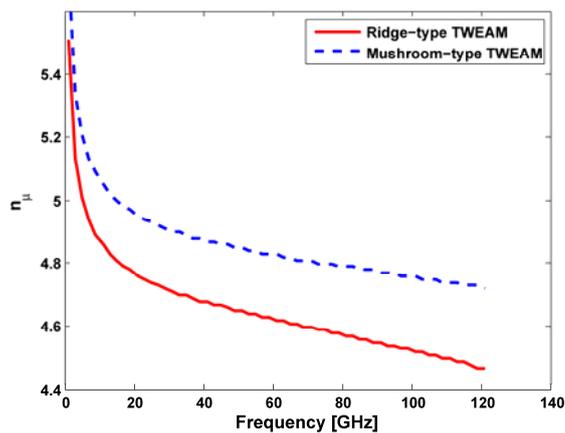


Fig. 11 Microwave refractive index vs. frequency.

Higher electro-optical response and speed indicates that better performance of mushroom-type is mainly due to the lower microwave loss.

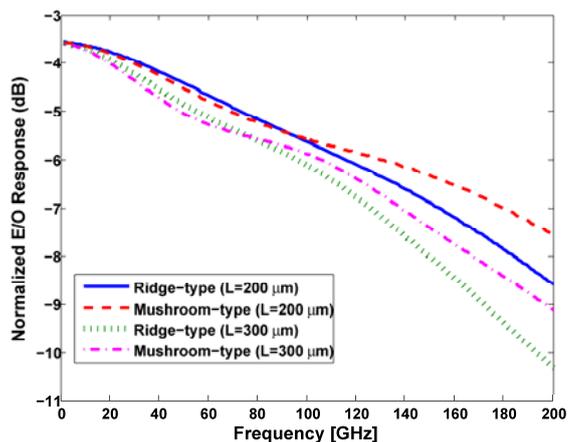


Fig. 12 Frequency response for ridge-type and mushroom-type TWEAM with different waveguide lengths.

### V. CONCLUSION

We have presented a full-vectorial finite-difference-based optical mode solver to analyze mushroom-type travelling wave electro-absorption modulator. Here, the discontinuities of the normal components of the electric field across abrupt dielectric interfaces have been considered in contrast to the scalar and semivectorial approximation methods. The important parameters in the high-frequency TWEAM design such as optical effective index which defines optical velocity and transverse mode confinement factor were calculated. The modulation response of mushroom-type TWEAM was calculated by

considering interaction between microwave and optical fields in waveguide and compared with conventional ridge-type TWEAM. Numerical values showed higher bandwidth for the mushroom-type TWEAM compared to the ridge-type of the same active region. The calculated 3dB bandwidths for ridge-type and mushroom-type TWEAM are about 139 GHz and 166 GHz for 200  $\mu\text{m}$  and 114 GHz and 126 GHz for 300  $\mu\text{m}$  waveguide length, respectively.

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